# Thermal Analysis of Neutral Beam Armor Array 

## NSTXU-CALC-11-05-00

September 22, 2011

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## PPPL Calculation Form

## Calculation \# NSTXU-CALC-11-05-00 Revision \# 00 WP \#, if any: 1707

(ENG-032)
Purpose of Calculation: (Define why the calculation is being performed.)

- To confirm beam source profile fit on NB Armor face
- To calculate beam divergence and armor-incidence effect on beam heat flux magnitude
- To use calculated fluxes to establish fault conditions, testing armor for $1 \& 2$ beamline fault cases
- To confirm that the armor cooling system will be sufficient to remove any residual heat from the armor during normal NSTX-U operations.
- To examine stainless steel backing plates in terms of thermal expansion during bake out (@ $150^{\circ} \mathrm{C}$ ) to ensure attached tiles to not interfere with each other.

References (List any source of design information including computer program titles and revision levels.)

- NSTX-U GRD (NB rev. 0 \& CS rev. 3)
- Microsoft Excel
- ALGOR
- ProE

Assumptions (Identify all assumptions made as part of this calculation.)

- Assumed a 1.5 vertical and .5 horizontal, half-angle divergence from last scraping surface for each beamline source.
- Assumed a max temp for ATJ tiles of $2600^{\circ}$ C. This reflects not a PHYSICAL limit, but rather one which avoids excessive sublimation of the carbon tiles.
- Assumed max tensile and compressive strengths of 26 MPa and 66MPa, respectively, for Graftech’s ATJ graphite, as stated in their material properties sheet. (http://graftech.com/getattachment/800b4a74-3229-4e44-a4ff-7b212ab06e24/GRAFSTAR\�\�\�-ATJ\�\�\�-Graphite.asp)

Calculation (Calculation is either documented here or attached): Attached

Conclusion (Specify whether or not the purpose of the calculation was accomplished.):
Source fit on armor face: this was confirmed by physically modeling the source profiles after calculating the geometry changes to their shapes due to beam divergence and the smearing effects of the incident angles. It was confirmed that all six sources fit comfortably on the armor, albeit, with some overlapping effects.

Divergence and incident angle effects on heat flux magnitude: this was calculated and used to convert input powers of 80, 90, and 110 kV into applicable heat fluxes, useful for modeling fault conditions. It was found that the overall area of the beam profile increases significantly from the last scrape-off surface as the beam diverges and smears along the armor. This reduces the overall magnitude of the heat flux. Values were calculated for both individual sources as well as heat flux values for the overlapping areas. Source heat flux was split into "hotspot" and "outer ring" zones, where the power density was 80 and $20 \%$ total power, respectively.

Beamline fault conditions and testing: it quickly became clear that, in the case of a single BL fault, ATJ graphite was an adequate material to provide protection for the vacuum vessel wall. The surface temperature never exceeded 2000C, much less the limit of 2600C. The internal stresses at the T-bar slot shoulder were found to be sufficiently low, leading to the belief that there would be no threat of critical crack formation in that sensitive zone. The principle stresses in the bulk of the tile and on the surface were also found to be low, well
within ATJ's published properties. If a single BL fault were to occur, the armor would survive without damage, barring any inherent weakness (unseen tile fractures, cracking). It would be recommended to attempt a visual inspection following the event as well as a complete maintenance event during the next outage.

However, for the double BL fault, the source overlap areas quickly exceeded ATJ graphite's limits for temperature and stress, generally passing this point after only $1 / 3$ into the length of the shot. The main danger here is not so much the surface temperature, but the stress at the shoulder of the T-bar slot. If the shoulder cracks and detaches, the whole tile could fall from the armor, exposing the stainless steel backing plate to neutral particles and possibly causing damage to other internal NSTX-U fixtures. To remedy this, Carbon-Fiber Composite (CFC) will replace ATJ as the tile material in those zones. CFC possesses tensile strengths 3 x that of ATJ as well as better thermal shock resistance. This material change will allow the armor to survive a double BL fault, probably with damage, but will allow the armor to successfully perform its duty as a sacrificial surface. As the fault strikes the armor, the tiles will rapidly heat, passing 2600C in $1 / 3$ of the shot length. The tile surface will begin to rapidly sublimate, but not fast enough to pose any concern about completely eroding a tile. If a double BL event occurs, physical inspection of the armor array is strongly recommended and replacement of one or more tiles will be likely.

Between-shot cooling during normal operations: this analysis confirmed that the flow rate and diameter of the present cooling system will be more than adequate for the upgrade thermal loading during normal operations.

Thermal growth of backing plates under thermal loading: the ALGOR analysis showed that under normal thermal loading, the greatest of which occurs during bakeout, the stainless steel backing plates grow "up and out" away from each other. Therefore, thermal loading of the plates poses no threat to the graphite/CFC tiles and the array will be able to flex and grow freely as it heats up during bakeout.

Cognizant Engineer's printed name, signature, and date
Kelsey Tresemer

I have reviewed this calculation and, to my professional satisfaction, it is properly performed and correct.
Checker's printed name, signature, and date

## Calculation

Introduction:
The Neutral Beamline Injection System (NBIS) Armor serves as a sacrificial protective surface for the neutral beamlines (NBs). With the addition of a second beamline, the armor went through a review and analysis to evaluate its performance with this increase to its mechanical and thermal requirements.

The upgrade proposal features the armor's counterclockwise movement inside the vacuum vessel to allow both sets of neutral beamline (NB) profiles to fit on the armor face. The beamlines overlap, causing areas of considerably increased heat flux, which were then analyzed for normal operations and fault conditions using simple tile shapes in ALGOR. The cooling lines were also analyzed for normal operational cooling with a simple simulation in ALGOR. Finally, the backing plates were analyzed to ensure that thermal growth during bakeout would not cause any interference between quadrants. The armor's mechanical capabilities were analyzed under a separate calculation.

## Explanation of Excel Calculation Sheet:

This portion of the NB armor calculation covers the NB source profiles, their mapping and the effect of the source divergence and surface smearing on the magnitude of the source heat flux. The heat flux gradients were also calculated in this file.

## Sheet 1: Determining Divergence in NBI 1 \& 2

The origin of the source was assumed to be from the last scrape-off surface, causing the source profile to assume a rectangular shape, 4.72 in by 17.32 in ( 12 cm by 44 cm ), with area of $81.84 \mathrm{in}^{2}\left(528 \mathrm{~cm}^{2}\right)$. The distances between the last scrape-off surface and the face of the NBI armor array was measured via ProE for each BL source. From this, assuming the vertical and horizontal half-angle beam divergence of 1.5 and .5 , respectively, the change in overall source profile dimensions was calculated, and the ratio of new area to old noted.

EXAMPLE: $\Delta$ in total dimension = distance from scrapeoff(tan (2*halfangle))

$$
\begin{aligned}
& \Delta d_{\text {total }}=311.521 * \tan (2 *(0.5)) \\
& \Delta d_{\text {total }}=5.437
\end{aligned}
$$

This is then added to the original dimension, resulting in the final horizontal and vertical size.
Sheet 2: Source "Smear"
As the beamline sources encounter the face of the armor, the incidence angle acts as a "smearing" surface, horizontally enlarging the source profile area. The diverged values from sheet 1 were run though this calculation which produced a new, "smeared" number for the horizontal dimension. The incident angle causes no vertical "smearing".

$$
\begin{aligned}
& \text { EXAMPLE: "smear" width = original width/sin(incidence angle) } \\
& \qquad \begin{aligned}
w_{\text {smear }} & =w_{o} / \sin (\theta) \\
w_{\text {smear }} & =10.162 / \sin \left(68.7^{\circ}\right) \\
w_{\text {smear }} & =10.907
\end{aligned}
\end{aligned}
$$

This sheet also contains the calculation which created the inner zone to the source profile. Rather than model the power distribution as a double Gaussian curve, a $20 \%$ reduction in size was estimated to contain $80 \%$ of the beam's power, and was thusly modeled.

Sheet 3: Source profile confirmation via photo data
In order to confirm the mathematical assumptions up until this point, the data from the sheets $1 \& 2$ were coMPared with photos taken of the NB armor, post-run. By measuring the areas where lithium was NOT deposited, we can get an idea of the total size and dimension of the source profile. Lithium evaporates at around

600 C, a number which coordinated to the hottest part of the source profile (or the $80 \%$ of the source). CoMParisons showed that the mathematical assumptions were $\sim 8 \%$ larger than the photograph.

Sheet 4: Ellipse Conversion
The true shape of the source profile as it encounters the armor is an ellipse, caused by divergence. Up until this point, the calculated dimensions have been simply the vertical height and the horizontal width of the profile. To properly represent the source shape, these values needed to be converted into an elliptical shape. Sheet 3 showed that ellipses created with these values will be $8 \%$ larger than in reality, which will affect the ultimate outcome of this analysis.

Formula for the area of an ellipse: $\pi a b$, where $a$ and $b$ are $\frac{1}{2}$ the width and height,respectively
By taking a ratio of the area of the source profile at the last scrape-off surface ( $81.84 \mathrm{in}^{2}$ ) and the elliptical area of the source profile as it encounters the armor face, after it has experienced divergence and smearing, a value was obtained to manipulate the magnitude of the beamline's heat flux.

$$
q_{\text {scrape off }}\left(\mathrm{MW} / \mathrm{m}^{2}\right)^{A_{0}} /_{A_{1}}=q_{\text {armor face }}
$$

This sheet also addresses the issue of when a source strikes the intersection of the two armor halves. This would cause the source profile to encounter two, different, incident angles, smearing the profile accordingly. To model these shapes in ProE, each portion of the source, or remnant, was treated as an entire unit, and smeared as per its respective angle. The profiles were applied to a global model of the NBI armor and the excess beam source trimmed away. The final width of each portion of source was recorded on this sheet.

At this point, the source profiles were applied to an armor model to confirm fit. Apart from some source overlap, all six profiles fit comfortably on the armor's face.


Figure 1. Confirming source profile fit on armor face

## NSTXU-CALC-11-05-00

Sheet 5: Heat Flux Magnitude
This sheet contains the calculation to apply the changes to the beam source profiles to the magnitude of the heat flux. At the last scraping surface, the heat flux per source is the equivalent to the source power (as defined by the shot parameters) divided by the area of the source. This heat flux was further broken down into $80 \%$ and $20 \%$ portions, to represent the hot spot and outer ring of power densities.

$$
\text { For a } 5 \text { sec, } 5 \mathrm{MW} \text { shot: }
$$

$$
\begin{gathered}
\frac{5 \mathrm{MW}}{3 \text { sources }}=1.67 \mathrm{MW} \\
\frac{1.67 \mathrm{MW}}{81.84 \mathrm{in}^{2}}=3.16 \mathrm{E} 07 \mathrm{MW} / \mathrm{in}^{2} \\
.80 * 3.16 \mathrm{E} 07=2.35 \mathrm{E} 07 \mathrm{MW} / \mathrm{in}^{2} \\
.20 * 3.16 \mathrm{E} 07=6.31 \mathrm{E} 06 \mathrm{MW} / \mathrm{in}^{2}
\end{gathered}
$$

From sheet 2, it was found that the source profiles experience both divergence and smearing, meaning that the source profile, when applied the face of the armor, increases in size. By taking a ratio of $A_{0} / A_{1}$, we can use this to modify the source profile's heat flux at the last scraping surface, and attain the at-armor-face heat flux.

$$
\begin{gathered}
\frac{A_{0}}{A_{1}}=\frac{81.84 \mathrm{in}^{2}}{264.46 \mathrm{in}^{2}}=.305 \\
(80 \%) \text { 2.35E07 } \mathrm{MW} / \mathrm{in}^{2} * .305=7.698 \mathrm{E} 06 \mathrm{MW} / \mathrm{in}^{2} \\
(20 \%) 6.34 \mathrm{E} 06 \mathrm{MW} / \mathrm{in}^{2} * .305=1.925 \mathrm{E} 06 \mathrm{MW} / \mathrm{in}^{2}
\end{gathered}
$$

Once these numbers were calculated for the hot spots and the outer rings, the overlap areas were identified using the ProE model of the armor and their respective heat flux magnitudes were computed. An area of particular concern is \#7, where three hot spots converge: BL2 B, BL2 A2, and BL1 C2.

Explanation of ALGOR analysis:
Once the heat fluxes for the armor were determined, it was then possible to construct scenarios for normal operations and possible fault conditions. During normal operation, the armor would see the same level of heat deposition as the rest of the First Wall devices, approximately $.06 \mathrm{MW} / \mathrm{m}^{2}$ average with $.13 \mathrm{MW} / \mathrm{m}^{2}$ peaking. This is very low-level heating and the armor would be under no threat of damage.

The fault conditions were split into two cases: single beam and double beam. A single beam fault would be the event in which a single beam fired into the armor in the absence of plasma in the vessel. The duration of such an event would be anywhere from a fraction of a second to 5 seconds. The magnitude of the applied heat flux would vary widely, with worst cases of $7.6 \mathrm{MW} / \mathrm{m}^{2}, 9.1 \mathrm{MW} / \mathrm{m}^{2}$, and $13.6 \mathrm{MW} / \mathrm{m}^{2}$ for 80,90 , and 110 kV , respectively. A double beam fault could see heat flux magnitudes of up to three times these values in areas of source overlap.

Assumptions:
Default nodal temperature: 20C
Ambient Temperature (for radiation): 60C
Element: Brick
Modeled with bricks and tetrahedrons
Material: ATJ graphite (material data file attached to Armor Analysis Excel file)
A single armor tile was modeled in ProE and, due to surface requirements of ALGOR, its top surface was sectioned to allow different heat flux values to be applied to different areas. This allowed the use of a single model for both single and double BL fault analyses. In ALGOR, the heat flux values generated in sheet 5 of the Excel analysis. For a single beamline fault, the entire surface of the tile was applied with the heat flux from
source BL1 C2 (highest heat flux of the six), for 80,90 , and 110 kV shots, for 5 , 3 , and 1 seconds long, respectively. This represented the "worst case" of the single BL faults. Radiation was enabled on the top surface as well (emissivity of 0.3 ). Each shot was allowed to run for the full time length and the max temperature and subsequent stresses recorded.

Table 1. ALGOR Single BL Fault Results

|  | time to <br> 2600 C | VonMises @ <br> 2600C (T-bar <br> slot) MPa | Max <br> Principle @ <br> 2600 <br> (overall) MPa | Time to 26 <br> MPa | Related <br> Max <br> Principle <br> MPa | Temp at 26 <br> MPa (VM) C |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 BL |  |  |  |  |  |  |
| 80 kV | $5.05 \mathrm{~s}:$ <br> 1781.40 | 15.88 | 13.19 | x | x | x |
| 90 kV | $3.08 \mathrm{~s}:$ <br> 1581.25 | 16.66 | 12.48 | x | x | x |
| 110 kV | $1.05 \mathrm{~s}:$ <br> 1285.10 | 18.43 | 11.29 | x | x | x |

A double BL fault utilized the sections cut into the surface and focused attention on the armor tile which was exposed to the greatest heat flux: tile C4. The heat flux applied to this tile corresponded with the overlap heat fluxes 4-9, listed on sheet 5 of the Excel analysis. Each of these heat fluxes were assigned to a section on the tile surface, with radiation enabled across the top surface as well (emissivity of 0.3). Runs were made of 80, 90 , and 110 kV heat fluxes, in an attempt to see how long before the tile surface a) reached 2600C and b) the internal stresses reached the limit of 26 MPa (tension).

Table 2. ALGOR Double BL Fault Results

|  | time to <br> 2600 C | VonMises @ <br> 2600C (T-bar <br> slot) MPa | Max <br> Principle @ <br> 2600 <br> (overall) MPa | Time to 26 <br> MPa | Related <br> Max <br> Principle <br> MPa | Temp at 26 <br> MPa (VM) C |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 BL |  |  |  |  |  |  |
| 80 kV | $2.44 \mathrm{~s}:$ <br> 2610.55 | 31.91 | 20.02 | $1.63 \mathrm{~s}: 25.90$ <br> MPa | 15.59 | 2083.65 |
| 90 kV | $1.73 \mathrm{~s}:$ <br> 2616.67 | 34.9 | 20.59 | $.978 \mathrm{~s}: 25.82$ <br> MPa | 14.47 | 1944.84 |
| 110 <br> kV | $.740 \mathrm{~s}:$ <br> 2601.23 | 37.53 | 21.36 | $.383 \mathrm{~s}: 25.16$ <br> MPa | 14.77 | 1804 |

## Cooling Line Evaluation

In order to evaluate the efficiency of the cooling lines imbedded into the stainless steel backing plates, a simple test piece was constructed to find the thermal time constant $\left(T_{c}\right)$ of the system, or, rather, to find the time it took for $63 \%$ of the heat in the system to be removed by the cooling system. A test piece was assembled in ProE which was a slice of ATJ tile, stainless steel backing plate, and embedded copper tube. In ALGOR, an initial temperature significantly higher than any the system would see during normal operations was applied to the entire assembly $(1000 \mathrm{C})$. The conditions of the cooling system were applied to the copper tube ( $3 / 8$ " dia., 3.6 GPM per backing plate) and the system left to run. The resulting graph was created and the time constant easily found: $\sim 50$ s.


Figure 2. ALGOR results of cooling line analysis.

This is simply an estimate in order to gain a perspective on how quick the majority of the heat within the armor can be removed. Since during normal operations the armor will only see a net heat gain of a few hundred degrees Celsius, as well as a between-shot cooling period of nearly 20 minutes, it is safe to deem the system adequate for use in NSTX-U.

## Backing Plate Thermal Growth

The mounting points for the armor underwent significant design changes, prompting an analysis of the armor's constraints and the manner in which it would mechanically respond to thermal loading. Since the amor array is symmetric about the horizontal and vertical axes, only a single quadrant's backing plate needed analysis. The plate was modeled in ProE and uploaded to ALGOR for testing. Since the highest temperatures the armor should ever see in normal operations would be during bake out, those conditions were simulated for the test. Hot helium was flowed through the cooling lines until the whole part reached ~350C and the consequent thermal growth was monitored and recorded. There was a chance that the plates could thermally grow towards one another, causing tile interference and possible fracturing and this needed confirmation.


Figure 3. ALGOR analysis of stainless steel backing plate thermal growth during bakeout: thermal heating


Figure 4. ALGOR analysis of stainless steel backing plate thermal growth during bakeout: mechanical growth

## NSTXU-CALC-11-05-00

## Conclusion

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Divergence and incident angle effects on heat flux magnitude: this was calculated and used to convert input powers of 80,90 , and 110 kV into applicable heat fluxes, useful for modeling fault conditions. It was found that the overall area of the beam profile increases significantly from the last scrape-off surface as the beam diverges and smears along the armor. This reduces the overall magnitude of the heat flux. Values were calculated for both individual sources as well as heat flux values for the overlapping areas. Source heat flux was split into "hotspot" and "outer ring" zones, where the power density was 80 and $20 \%$ total power, respectively.

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## NSTXU-CALC-11-05-00

## Appendix A: Excel Analysis

Excel Sheet 1


## NSTXU-CALC-11-05-00

Excel Sheet 2

| Deter | ing Bea | am Smear On Arm | nor Face |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Current Beam Line |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | Beam | line |  |  |  |
| Constant |  | cm |  |  |  |  |  |  |  |  | $!$ ! | $!!$ | 1 |  |  |
| beam w | 4.724 | 12 |  | in^2 | $\mathrm{cm}^{\wedge} 2$ |  |  |  |  |  | I | $!$ ! | I |  |  |
| beam h | 17.323 | 44 | Area | 81.84016368 | 528 |  |  |  |  |  | 1 I | 1 ! | I |  |  |
|  |  |  |  |  |  |  |  |  |  |  | i | $\downarrow$ |  |  |  |
|  | inches |  |  |  | cm |  |  |  |  |  |  |  |  |  |  |
|  | beam w | beam h |  |  | beam w | beam h |  |  |  |  | 11 |  | I |  |  |
| B1A | 10.162 | 33.638 |  | B1A | 25.811 | 85.440 |  |  |  |  | 1 | 1 I | I |  |  |
| B1B | 10.176 | 33.682 |  | B1B | 25.848 | 85.551 |  |  |  |  |  |  |  |  |  |
| B1C | 10.244 | 33.886 |  | B1C | 26.021 | 86.071 |  |  |  |  |  | $\dot{i}$ | $\dot{\nu}$ |  |  |
| B2A | 9.792 | 32.529 |  | B2A | 24.872 | 82.624 |  |  |  | $\leftarrow$ |  | mw | $\square$ |  |  |
| B2B | 9.924 | 32.926 |  | B2B | 25.208 | 83.632 |  |  |  |  |  |  |  |  |  |
| B2C | 10.040 | 33.274 |  | B2C | 25.502 | 84.516 |  |  |  |  |  |  | ( |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | Beam Line | Incidence Angle ( $\theta$ ) | smear width | height | $\mathrm{A}_{0} / \mathrm{A}_{1}$ |  | smear width | height |  |  |  |  |  |  |  |
|  |  |  | inch | hes |  |  | cm |  |  |  |  |  |  |  |  |
| BL1 | $\mathrm{B}_{1} \mathrm{~A}$ | 68.7 | 10.91 | 33.638 | 0.284 |  | 27.703 | 85.440 |  |  |  |  |  | - |  |
|  | $\mathrm{B}_{1} \mathrm{~B}$ | 64.7 | 11.26 | 33.682 | 0.275 |  | 28.590 | 85.551 |  |  |  |  |  |  |  |
|  | $\mathrm{B}_{1} \mathrm{C}_{1}$ | 60.7 | 11.75 | 33.886 | 0.262 |  | 29.838 | 86.071 |  |  |  |  |  |  |  |
|  | $\mathrm{B}_{1} \mathrm{C}_{2}$ | 94.3 | 10.27 | 33.886 | 0.299 |  | 26.094 | 86.071 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| BL2 | $\mathrm{B}_{2} \mathrm{~A}_{1}$ | 25.6 | 22.66 | 32.529 | 0.141 |  | 57.562 | 82.624 |  |  |  |  |  |  |  |
|  | $\mathrm{B}_{2} \mathrm{~A}_{2}$ | 39.4 | 15.43 | 32.529 | 0.208 |  | 39.185 | 82.624 |  |  |  |  |  |  |  |
|  | $\mathrm{B}_{2} \mathrm{~B}$ | 43.4 | 14.44 | 32.926 | 0.219 |  | 36.688 | 83.632 |  |  |  |  |  |  |  |
|  | $\mathrm{B}_{2} \mathrm{C}$ | 47.4 | 13.64 | 33.274 | 0.230 |  | 34.645 | 84.516 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Adjust nu | mber for a | \% reduction in size tor | to represent | nner "hotspot" | " (80\% total | power) |  |  |  |  |  |  |  |  |  |
|  | Beam Line |  | width | height |  |  | smear width | height |  |  |  |  |  |  |  |
|  |  |  | inch | hes |  |  | cm |  |  |  |  |  |  |  |  |
| BL1 | $\mathrm{B}_{1} \mathrm{~A}$ |  | 8.725 | 26.910 |  |  | 22.162 | 68.352 |  |  |  |  |  |  |  |
|  | $\mathrm{B}_{1} \mathrm{~B}$ |  | 9.005 | 26.945 |  |  | 22.872 | 68.441 |  |  |  |  |  |  |  |
|  | $\mathrm{B}_{1} \mathrm{C}_{1}$ |  | 9.398 | 27.109 |  |  | 23.870 | 68.857 |  |  |  |  |  |  |  |
|  | $\mathrm{B}_{1} \mathrm{C}_{2}$ |  | 8.219 | 27.109 |  |  | 20.875 | 68.857 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| BL2 | $\mathrm{B}_{2} \mathrm{~A}_{1}$ |  | 18.130 | 26.023 |  |  | 46.050 | 66.099 |  |  |  |  |  |  |  |
|  | $\mathrm{B}_{2} \mathrm{~A}_{2}$ |  | 12.342 | 26.023 |  |  | 31.348 | 66.099 |  |  |  |  |  |  |  |
|  | $\mathrm{B}_{2} \mathrm{~B}$ |  | 11.555 | 26.341 |  |  | 29.351 | 66.906 |  |  |  |  |  |  |  |
|  | $\mathrm{B}_{2} \mathrm{C}$ |  | 10.912 | 26.619 |  |  | 27.716 | 67.612 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| *We | ume that p | ower density falls off | at the edges o | of the beam |  |  |  |  |  |  |  |  |  |  |  |
| line | ue to diven accep | gence in the beam. A ted as a model of pow | 20-80 division wer density. | has been |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Excel Sheet 3


## NSTXU-CALC-11-05-00

Excel Sheet 4

## Ellipse Conversion



Excel Sheet 5

| Heat Flux Per Tile |  |  |  |  |  |  |  |  |  |  | $\mathrm{A}_{0} / \mathrm{A}_{1}$ | ( $\mathrm{W} / \mathrm{m}^{\wedge} 2$ ) |  | Overlap heat fluxes |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 12345678 |  |  |  |  |  |  |  |  | HS power OD power |  | 1 | $\begin{aligned} & 8.617 \mathrm{E}+06 \\ & 1.360 \mathrm{E}+07 \end{aligned}$ |  | $2 \mathrm{CHS}+2 \mathrm{BOD}$ |  |
|  |  |  |  |  | BL1 |  | B1A |  | 0.284 | $8.607 \mathrm{E}+06$ |  | $2.152 \mathrm{E}+06$ |  | 2 |  | $2 \mathrm{CHS}+2 \mathrm{BHS}$ |  |
| A |  |  |  |  |  |  |  | Time (sec) |  |  | B1B |  | 0.275 | $8.329 \mathrm{E}+06$ | $2.082 \mathrm{E}+06$ | 3 | $8.379 \mathrm{E}+06$ |  | $2 \mathrm{COD}+2 \mathrm{BHS}$ |  |
| B |  |  |  |  |  |  | 0.75 |  |  | B1C1 |  | 0.262 | $7.932 \mathrm{E}+06$ | $1.983 \mathrm{E}+06$ | 4 | $8.212 \mathrm{E}+06$ |  | $2 \mathrm{BHS}+2 \mathrm{~A} 2 \mathrm{OD}$ |  |
| C |  |  |  |  |  |  |  |  | B1C2 |  | 0.299 | $9.070 \mathrm{E}+06$ | $2.268 \mathrm{E}+06$ | 5 | 8.617E+06 |  | $2 \mathrm{BHS}+2 \mathrm{~A} 2 \mathrm{HS}$ |  |
| D |  |  |  |  |  | FAULT |  |  |  |  |  |  |  | 6 | $1.520 \mathrm{E}+07$ |  | $2 \mathrm{BHS}+2 \mathrm{~A} 2 \mathrm{HS}+$ |  |
| E |  |  |  |  |  | q (heat flux W/m^2) |  | BL2 | B2A1 |  | 0.141 | $4.283 \mathrm{E}+06$ | $1.071 \mathrm{E}+06$ | 7 | $2.200 \mathrm{E}+07$ |  | $2 \mathrm{BHS}+2 \mathrm{~A} 2 \mathrm{HS}+$ |  |
| F |  |  |  |  |  | $3.79 \mathrm{E}+07$ |  |  | B2A2 |  | 0.208 | $6.292 \mathrm{E}+06$ | $1.573 \mathrm{E}+06$ | 8 | $1.702 \mathrm{E}+07$ |  | $2 \mathrm{BOD}+2 \mathrm{~A} 2 \mathrm{HS}$ |  |
|  |  |  |  |  |  | HotSpot (80\%) |  |  | B2B |  | 0.219 | $6.639 \mathrm{E}+06$ | $1.660 \mathrm{E}+06$ | 9 | $1.536 \mathrm{E}+07$ |  | $2 \mathrm{~A} 2 \mathrm{HS}+1 \mathrm{C} 2 \mathrm{HS}$ |  |
|  |  |  |  |  |  | $3.03 \mathrm{E}+07$ |  |  | B2C |  | 0.230 | $6.957 \mathrm{E}+06$ | $1.739 \mathrm{E}+06$ | 10 | $1.222 \mathrm{E}+07$ |  | $2 \mathrm{~A} 1 \mathrm{HS}+1 \mathrm{C} 1 \mathrm{HS}$ |  |
|  |  |  |  |  |  | OuterRing(20\%) |  |  |  |  |  |  |  | 11 | $1.430 \mathrm{E}+07$ |  | $2 \mathrm{~A} 1 \mathrm{HS}+1 \mathrm{C} 1 \mathrm{HS}$ |  |
|  |  |  |  |  |  | $7.58 \mathrm{E}+06$ |  |  |  |  |  |  |  | 12 | $1.460 \mathrm{E}+07$ |  | $2 \mathrm{~A} 1 \mathrm{HS}+1 \mathrm{C} 10 \mathrm{D}$ |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  | 13 | $6.366 \mathrm{E}+06$ |  | $2 \mathrm{~A} 1 \mathrm{HS}+1 \mathrm{BOD}$ |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  | 14 | $1.261 \mathrm{E}+07$ |  | $2 \mathrm{~A} 1 \mathrm{HS}+1 \mathrm{BHS}$ |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  | 15 | $9.400 \mathrm{E}+06$ |  | $2 \mathrm{~A} 10 \mathrm{D}+1 \mathrm{BHS}$ |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  | 16 | $1.048 \mathrm{E}+07$ |  | $1 \mathrm{BHS}+1 \mathrm{AOD}$ |  |
|  |  |  |  |  |  |  | NBI Power to Plasma/Beam line |  |  |  |  |  |  | 17 | $1.069 \mathrm{E}+07$ |  | $1 \mathrm{BOD}+1 \mathrm{AHS}$ |  |
|  |  |  |  |  |  |  |  | Pulse Length (s) | Power to plasma (MW) | 2 NB | power/source (MW) q (per source, W/m^2) |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 5.00 | 5 | 10 | 1.67 | $3.16 \mathrm{E}+07$ | 80 kV |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 4.00 | 5.4 | 10.8 | 1.80 | $3.41 \mathrm{E}+07$ |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 0.0528 | 3.00 | 6 | 12 | 2.00 | $3.79 \mathrm{E}+07$ | 90 kV |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 2.00 | 6.8 | 13.6 | 2.27 | $4.29 \mathrm{E}+07$ |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 1.50 | 7.5 | 15 | 2.50 | $4.73 \mathrm{E}+07$ |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 1.25 | 8.2 | 16.4 | 2.73 | $5.18 \mathrm{E}+07$ |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 1.00 | 9 | 18 | 3.00 | $5.68 \mathrm{E}+07$ | 110 kV |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | MSE |  | power/source (MW) | q (per source, | W/m^2) |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | 1.67 | $1.40 \mathrm{E}+07$ |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | 2.00 | $1.90 \mathrm{E}+07$ |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | 3.00 | $2.80 \mathrm{E}+07$ |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Excel Sheet 6

| ALGOR results |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | time to 2600C | VonMises @ 2600C (tbar slot) Mpa | Max Principle @ 2600 (overall) Mpa | Time to 26 Mpa | Related Max <br> Principle Mpa | Temp at 26 MPa (VM) C |  |
| 1 BL |  |  |  |  |  |  |  |
| 80 kV | 5.05s: 1781.40 | 15.88 | 13.19 | x | x | x |  |
| 90 kV | 3.08s: 1581.25 | 16.66 | 12.48 | $x$ | x | x |  |
| 110 kV | 1.05s: 1285.10 | 18.43 | 11.29 | x | x | x |  |
|  | time to 2600C | VonMises @ 2600C (tbar slot) Mpa | Max Principle @ 2600 (overall) Mpa | Time to 26 Mpa | Related Max <br> Principle Mpa | Temp at 26 MPa (VM) C |  |
| 2 BL |  |  |  |  |  |  |  |
| 80 kV | 2.44s: 2610.55 C | 31.91 | 20.02 | 1.63s: 25.90 Mpa | 15.59 | 2083.65 |  |
| 90 kV | 1.73s: 2616.67C | 34.9 | 20.59 | .978s: 25.82 Mpa | 14.47 | 1944.84 |  |
| 110 kV | .740s: 2601.23 | 37.53 | 21.36 | .383S: 25.16 Mpa | 14.77 | 1804 |  |
|  |  |  |  |  |  |  |  |

Excel Sheet 7

|  | Temp © | kx | ky | kz | Sp |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 116 | 116 | 116 | 711 |  | k $=$ thermal | al conductivity | vity (W/mk) |  |
|  | 27 | 116 | 116 | 116 | 711 |  |  |  |  |  |
|  | 127 | 106 | 106 | 106 | 975 |  |  |  |  |  |
|  | 227 | 95 | 95 | 95 | 1185 |  |  |  |  |  |
|  | 527 | 75 | 75 | 75 | 1600 |  |  |  |  |  |
|  | 1027 | 50 | 50 | 50 | 1865 |  |  |  |  |  |
|  | 1527 | 43 | 43 | 43 | 1975 |  |  |  |  |  |
|  | 2027 | 42 | 42 | 42 | 2050 |  |  |  |  |  |
|  | 2627 | 40 | 40 | 40 | 2060 |  |  |  |  |  |
|  | 3027 | 40 | 40 | 40 | 2075 |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |

## Appendix B: ALGOR Results



80 kV Von Mises Stress


80 kV Max Principle Stress


90 kV , 3s


90 kV Von Mises Stress


90 kV Max Principle Stress


## 110 kV , 1s



## 110 kV, Von Mises Stress



## 110 kV, Max Principle Stress



80 kV, 2 BL @ 2600C


80 kV, 2 BL @ 2600C, Von Mises

$80 \mathrm{kV}, 2$ BL @ 2600C, Max Principle


80 kV, 2 BL@ 26 Mpa Von Mises


80 kV, 2 BL @ 26 Mpa Von Mises


80 kV, 2 BL @ 26 Mpa Von Mises, Max Principle


90 kV, 2 BL @ 2600 C


90 kV, 2 BL @ 2600 C, Von Mises


90 kV, 2 BL @ 2600 C, Max Principle


90 kV, 2 BL @ 26 Mpa Von Mises


90 kV, 2 BL @ 26 Mpa Von Mises


90 kV, 2 BL @ 26 Mpa Von Mises, Max Principle


110 kV, 2 BL @ 2600 C


110 kV, 2 BL @ 2600 C, Von Mises


110 kV, 2 BL @ 2600 C, Max Principle


110 kV, 2 BL @ 26 Mpa Von Mises


110 kV, 2 BL @ 26 Mpa Von Mises


110 kV, 2 BL @ 26 Mpa Von Mises, Max Principle


Cognizant Engineer's printed name, signature, and date

I have reviewed this calculation and, to my professional satisfaction, it is properly performed and correct.
Checker's printed name, signature, and date

